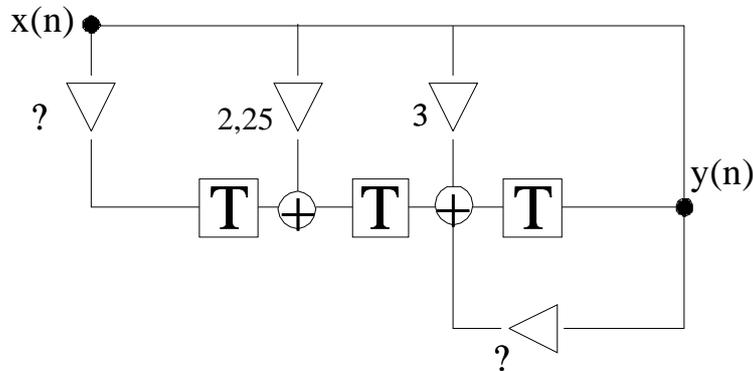


Digital Signal Processing: Deterministic Signals

1. System analysis

1.1. We look again at the digital filter from the „foundations“ experiment.



1.2. Is the filter stable? Is the filter causal?

1.3. What type of filter do we have (low-pass, high-pass, all-pass, band-pass, inverse band-pass?)

1.4. Our periodic series $x(n) = [0, 2, 0, -2, 0, 2, 0, -2, \dots]$ is now to be understood as a sampling of a signal $x(t) = A \cdot \sin(2\pi f t)$ at times $t = nT$. What is the amplitude A , the frequency f and the sampling time T ? Is this result unique?

1.5. According to the sampling theorem, what minimum sampling frequency $F_s = 1/T$ is needed to fully recover the signal?

2. MATLAB Computer experiments

2.1. From $H(z)$, let Matlab compute the frequency response $H(f)$ of the filter. Let Matlab draw a sketch of $|H(f)|$ and of $\arg H(f)$. All need is the function *freqz*.

2.2. Now modify one of the poles in such a way that the filter becomes non-causal. Again, let Matlab draw a sketch of $|H(f)|$ and of $\arg H(f)$.

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2.3. For the modified $H(z)$, let Matlab perform an inverse z-Transformation in two ways:

a) to give you the corresponding difference equation

b) inverse-transforming the steady state part and the initial part.

2.4. We use the periodic series $[0, 2, 0, -2, 0, 2, 0, -2, \dots]$ again. Pass a long series of this nature to the modified filter. What is the output after some time?

2.5. Is there a steady state? What does it look like?

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2.6. The signal $x(t) = A \cos(2\pi f t)$, with $t = 0:0.01:5$ is given.

- 2.7. Let Matlab sample the signal $x(t)$ with frequencies f_a below and above F_s (use `abstast(x,t,f_a)`).
- 2.8. Compute the spectrum of the sampled signal. Discuss aliasing. Use:
`y=cos(2*pi*(0:1/f_a:max(t))*F); % cos-function only with the sampling points`
`Y=fft(yy,FFT_length) with FFT_length=512`
- 2.9. Repeat the sampling, but this time only a window of length $n=5$ is known to the observer.
`y2=y(1:n);`
In this range, apply a rectangular window (`rectwin(N)`) and a Hamming (`hamming(N)`) window. Plot the spectrum and discuss the differences between the three situations.
a) no window (2.6.), b) rectangular window $n=5$, c) Hamming window $n=5$.